

2D CONCURRENT FORCES:

- all lines of action intersect at a single point
- no moment (torque) / (ROTATION)

EQUILIBRIUM:

Newton's 2nd Law: $F = m \cdot a$

IN A STATIC SYSTEM $a = 0$

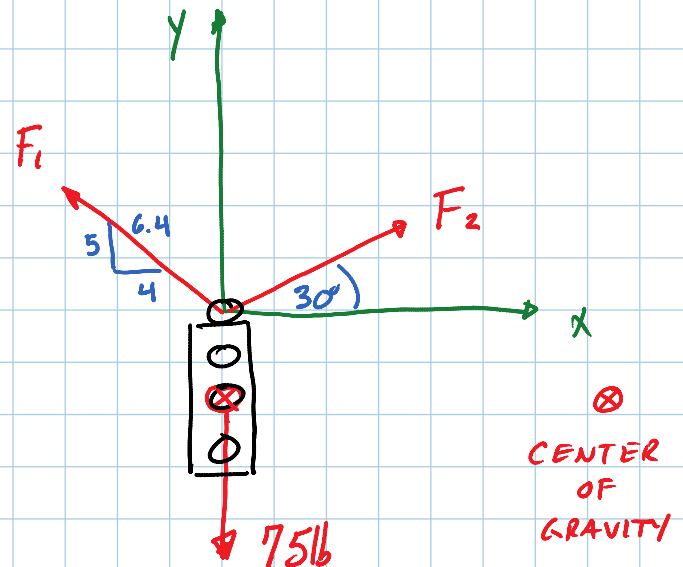
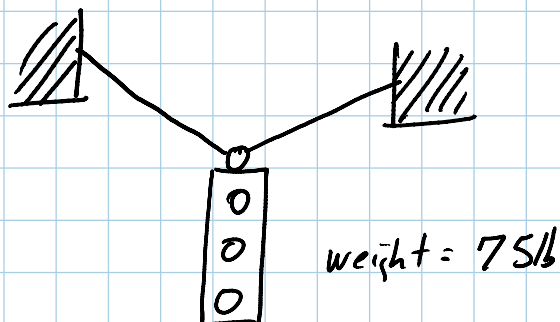
$$\therefore F = m \cdot 0 \Rightarrow F = 0?$$

$\Sigma F = 0$ IN STATIC EQUILIBRIUM

$\Sigma F_x = 0$ if not there is a net force in the x-direction, and the object is moving in the x-direction

$$\Sigma F_y = 0$$

$$\Sigma F_z = 0$$



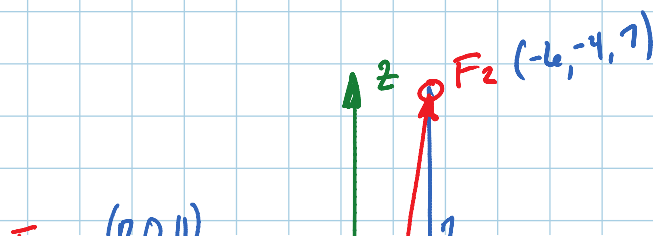
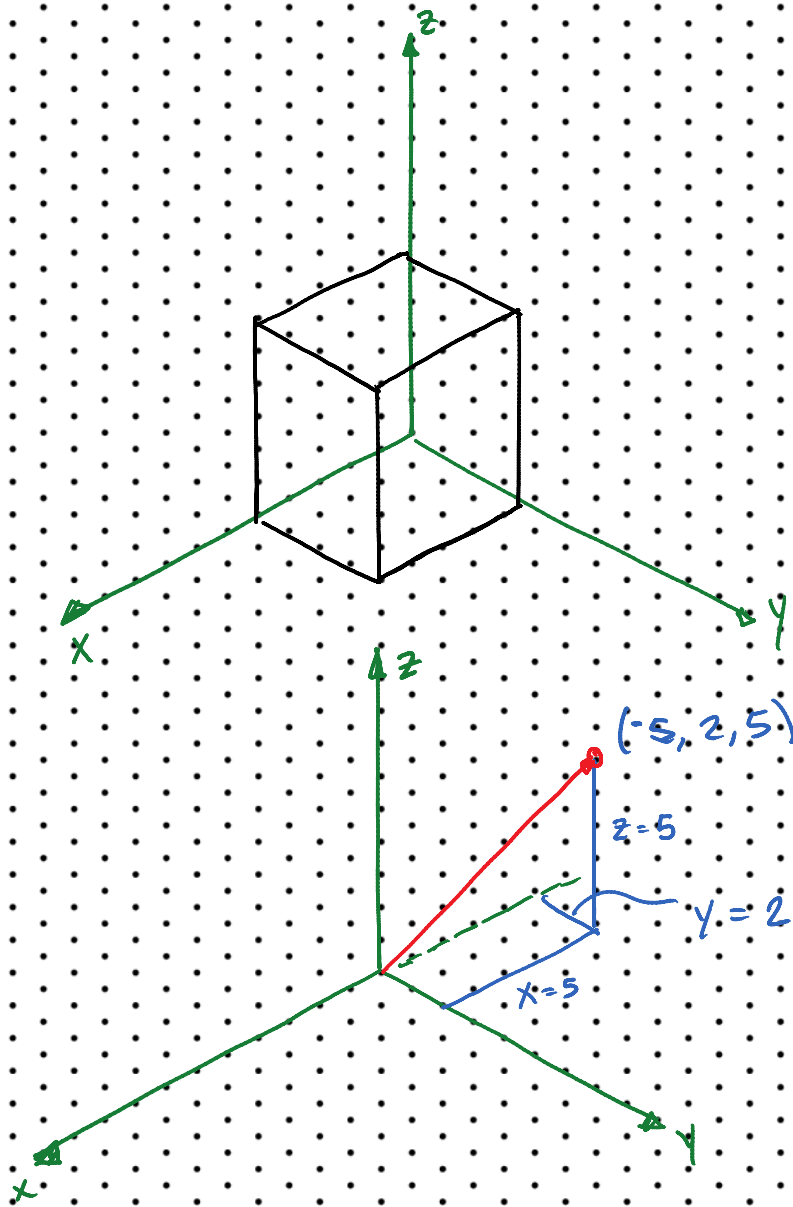
$$\Sigma F_x = 0 = F_2 \cdot \cos 30^\circ - F_1 \cdot \cos \theta$$

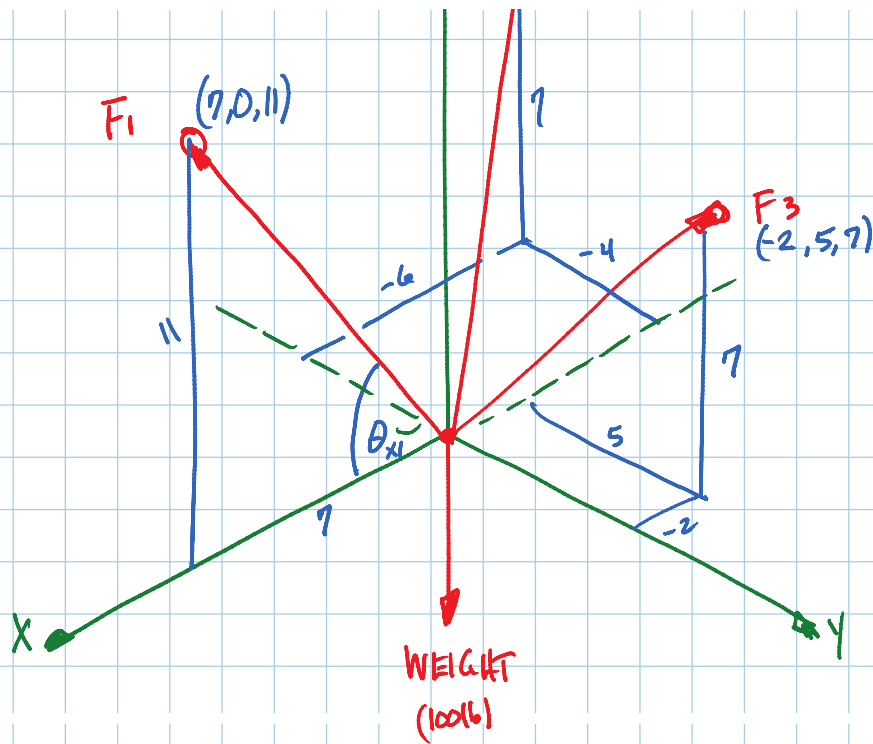
$$0 = F_2 \cdot \cos 30^\circ - F_1 \cdot \frac{4}{6.4}$$

$$\sum F_y = 0 = F_2 \cdot \sin 30^\circ + F_1 \cdot \frac{5}{6.4} - 75 \text{ lb}$$

$$F_2 = 47.4 \text{ lb} \quad F_1 = 65.7 \text{ lb}$$

Isometric Dot paper





$$L_1 = \sqrt{7^2 + 0^2 + 11^2} = 13.04$$

$$L_2 = \sqrt{-6^2 + -4^2 + 7^2} = 10.05$$

$$L_3 = \sqrt{-2^2 + 5^2 + 7^2} = 8.83$$

$$\Sigma F_x = 0 = F_{1x} + F_{2x} + F_{3x}$$

$$= F_1 \cdot \cos \theta_{x1} + F_2 \cdot \cos \theta_{x2} + F_3 \cdot \cos \theta_{x3}$$

$$\begin{aligned} 0 &= F_1 \cdot \frac{7}{13.04} + F_2 \cdot \frac{-6}{10.05} + F_3 \cdot \frac{-2}{8.83} \\ \Sigma F_y = 0 &= F_1 \cdot \frac{0}{13.04} + F_2 \cdot \frac{-4}{10.05} + F_3 \cdot \frac{5}{8.83} \\ \Sigma F_z = 0 &= F_1 \cdot \frac{11}{13.04} + F_2 \cdot \frac{7}{10.05} + F_3 \cdot \frac{7}{8.83} - 100 \text{ lb} \end{aligned}$$

$$\begin{bmatrix} 0 \\ 0 \\ 100 \end{bmatrix} \text{ lb} = \begin{bmatrix} 0.537 & -0.597 & -0.227 \\ 0 & -0.398 & 0.566 \\ 0.844 & 0.697 & 0.793 \end{bmatrix}$$

[B]

[A]

$$[A]^{-1} \cdot [B] = \begin{bmatrix} F_1 \\ F_2 \\ F_3 \end{bmatrix} = \begin{bmatrix} 57.7 \\ 70.9 \\ 28.8 \end{bmatrix} \text{ lb}$$